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## DC / AC Formulae

$$1 \text{ C} = 6.24 \times 10^{18} \text{ electrons}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$\mu_0 = 1.26 \times 10^{-6} \text{ H/m}$$

$$1 \text{ HP} = 746 \text{ W}$$

$$1 \text{ in.} = 2.54 \text{ cm}$$

$$1 \text{ mi.} = 5280 \text{ ft.}$$

$$1 \text{ kg} = 2.2 \text{ lb.}$$

$$F = \frac{1}{4\pi\epsilon} \times \frac{Q_1 Q_2}{d^2}$$

$$W = Fd = QV$$

$$Q = It$$

$$E = IR$$

$$P = \frac{W}{t}$$

$$P = VI = I^2R = \frac{V^2}{R}$$

$$\eta = \frac{P_o}{P_i}$$

$$R = \frac{\rho l}{A}$$

$$G = \frac{1}{R}$$

$$R_{\text{new}} = R_{20^\circ\text{C}}(1 + \alpha\Delta T)$$

$$\Delta T = (T_{\text{new}} - 20^\circ\text{C})$$

$$D = \frac{\Psi}{A}$$

$$E = \frac{E}{q} = \frac{E}{d}$$

$$\epsilon = \frac{D}{E}$$

$$\epsilon = \epsilon_r \epsilon_0$$

$$Q =$$

$$= \frac{Q}{f}$$

$$i_C = C \frac{dV}{dt}$$

$$W = \frac{1}{2} CV^2$$

$$\tau = RC = \frac{L}{R}$$

$$v = V_f - (V_f - V_i) e^{-t/\tau}$$

$$i = I_f - (I_f - I_i) e^{-t/\tau}$$

$$f_c = \frac{1}{2\pi\tau}$$

$$\tau_r = 2.2\tau$$

$$F = NI = HI$$

$$B = \frac{\mu}{A}$$

$$\mu = \frac{B}{H}$$

$$\mu = \mu_r \mu_0$$

$$L = \frac{\mu N^2 A}{l}$$

$$v_L = \frac{d\psi}{dt} = N \frac{d\phi}{dt}$$

$$e_{\text{ind}} = -L \frac{di}{dt}$$

$$W = \frac{1}{2} LI^2$$

$$a = \frac{dv}{dt} \sin(\omega t + \phi)$$

$$v_{\text{avg}} (\text{half cycle}) = \frac{2V_p}{\pi}$$

$$V_{\text{rms}} = \frac{V_p}{\sqrt{2}} = \frac{V_{\text{avg}}}{2\sqrt{2}}$$

$$\omega = 2\pi f$$

$$T = \frac{1}{f}$$

$$X_L = 2\pi fL$$

$$X_C = \frac{1}{2\pi fC}$$

$$Z = R \pm jX$$

$$Y = G \pm jB$$

$$Y = \frac{1}{Z} \quad G = \frac{1}{R} \quad B = \frac{1}{X}$$

$$S = P + jQ$$

$$= \cos \theta$$

$$Q_{\text{total}} = \frac{X_L}{R_X}$$

$$Q_Y = \frac{X_L \text{ or } X_C}{R_{\text{tot}}}$$

$$P = \frac{Q_L \text{ or } Q_C}{F}$$

$$Q_N = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$Q_P = \frac{R_{\text{tot}}}{X_L \text{ or } X_C}$$

$$Q_F = R \sqrt{\frac{C}{L}}$$

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

$$f_r = \sqrt{f_1 f_2}$$

$$BW = \frac{f_c}{Q} = (f_2 - f_1)$$

$$f_1 = f_r - \frac{BW}{2}$$

$$f_2 = f_r + \frac{BW}{2}$$

$$R_P = R_S(1 + Q^2)$$

$$X_P = X_S \left(1 + \frac{1}{Q^2}\right)$$

$$f_r = \frac{1}{2\pi\sqrt{LC}} \sqrt{1 - \frac{R_S^2 C}{L}}$$

$$a = \frac{B_C}{N_S} = \frac{V_C}{V_S} = \frac{I_S}{I_P} = \sqrt{\frac{Z_C}{Z_S}}$$

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## Devices Formulae

### Diode Circuits

$$I_F = \frac{E - V_F}{R} \quad I_R = \frac{E - V_R}{R}$$

### BJT Equations

$$\beta = \frac{I_C}{I_B} \quad \alpha = \frac{I_C}{I_E} \quad \beta = \frac{\alpha}{1 - \alpha} \quad \alpha = \frac{\beta}{\beta + 1}$$

$$I_E = I_C + I_B \quad V_{CE} = V_{CEB} + V_{EB}$$

$$h_{ib} = \frac{26 \text{ mV}}{I_B} + r_e \quad r_e = 10 \Omega, \text{ if not given}$$

$$h_{ie} = (h_{FE} + 1) h_{ib}$$

$r_e$  = external ac resistance looking **out** the emitter

$r_b$  = external ac resistance looking **out** the base

$r_c$  = external ac resistance looking **out** the collector

### Common Emitter Amplifiers

$$R_i' = (h_{FE} + 1)(h_{ib} + r_e)$$

$$R_i = R_1 \parallel R_2 \parallel R_i'$$

$$R_o' = \infty$$

$$R_o = R_C \parallel R_o' = R_C$$

$$A_v = \frac{-R_C \parallel R}{(h_{ib} + r_e)} = \frac{-r_c}{(h_{ib} + r_e)}$$

$$A_i = \frac{A_v R_i}{R} \quad A_P = A_v A_i$$

### Emitter Follower Amplifier

$$R_i' = (h_{FE} + 1)(h_{ib} + r_e)$$

$$R_i = R_1 \parallel R_2 \parallel R_i'$$

$$R_o' = \frac{h_{ib} + r_e \parallel R_1 \parallel R_2}{h_{FE} + 1}$$

$$R_o = R_o' \parallel R_E$$

$$A_v = \frac{r_e}{h_{ib} + r_e}$$

$$A_i = \frac{A_v R_i}{R} \quad A_P = A_v A_i$$

### Amplifier Design Rules

$$V_{CE} = 0.1 \times V_{CC} \quad V_{CE} = 0.5 \times V_{CC}$$

$$R_2 = 10 \times R_E$$

### Decibel Relationships

$$A_{p(dB)} = 10 \log \left( \frac{P_o}{P_i} \right)$$

$$A_{v(dB)} = 20 \log \left( \frac{V_o}{V_i} \right)$$

$$A_{i(dB)} = 20 \log \left( \frac{I_o}{I_i} \right)$$

$$A_{v(dB)} = 10 \log \left( \frac{P_o}{1.0 \text{ mW}} \right)$$

### Amplifier Measurement Model

$$V_o = \frac{V_{in} - V_i}{R_{in} + R} = \frac{V_{in}}{R}$$

$$R_i = \frac{V_i}{I_i} = \frac{R_{in} + R}{V_o - V_i}$$

$$R_o = \frac{V_{oc} - V_o}{I_o} = \frac{(V_{oc} - V_o) R}{V_o}$$

### BJT Switching

$$I_C(\text{sat}) = \frac{V_{CC} - V_{CE}(\text{sat})}{R_C}$$

$$I_B(\text{sat}) = \frac{I_C(\text{sat})}{\beta}$$

$$V_o(\text{sat}) = V_{CE} + V_{CE}(\text{sat})$$

### Op Amp Frequency Response

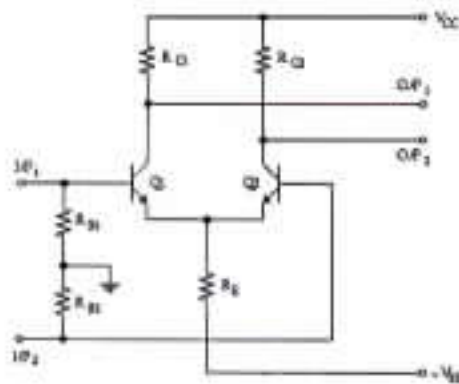
$$f_c = \frac{1}{2\pi RC}$$

Factor for 'n' identical stages:  $\sqrt{2^{1/n} - 1}$

$$\text{slope} = \frac{dB_{HF} - dB_{LF}}{\log HF - \log LF} = \frac{dB_{HF} - dB_{LF}}{\log \left( \frac{HF}{LF} \right)}$$

$$GBP = A_{v_o} \times BW \quad \text{where} \quad A_{v_o} = \frac{R_L + 1}{R_1}$$

### Differential Amplifiers



$$V_{B1} = V_{B2} = 0 \text{ V}$$

$$I_E (\text{total}) = \frac{V_E - V_{EE}}{R_E} \quad I_{C1} = I_{C2} = \frac{I_E (\text{total})}{2}$$

$$V_{C1} = V_{C2} = V_{CC} - I_C R_C$$

$$v_{O1} = v_{O2} = 0 \text{ V}$$

$$v_{O1} = v_{O2} = 0 \text{ V}$$

$$v_{IC} = \frac{v_{O1} + v_{O2}}{2}$$

$$v_{IC} = v_{O1} A_{VDD} + v_{O2} A_{VCC}$$

$$v_{I1} = v_{IC} + \frac{v_{O1}}{2}$$

$$v_{I2} = v_{IC} - \frac{v_{O1}}{2}$$

$$A_{VDD} = \frac{v_{O1}}{v_{I1}} \text{ or } \frac{v_{O2}}{v_{I2}}$$

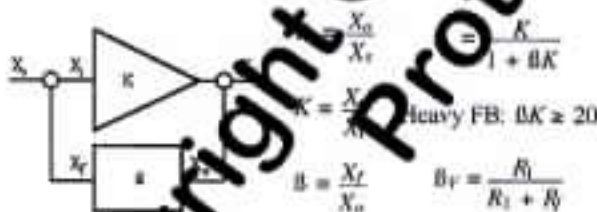
$$A_{VDD} = \frac{v_{O1}}{v_{I1}} = 2 A_{VCC}$$

$$A_{VCC} = \frac{v_{O1}}{v_{I2}} \text{ or } \frac{v_{O2}}{v_{I1}}$$

$$CMRS = \frac{A_{VDD}}{A_{VCC}}$$

$$CMRS_{dB} = 20 \log CMRS$$

### Feedback Amplifiers



### Feedback Effects on Impedance

$$R_{OY} = \frac{R_O}{BK} \quad \text{sampling output voltage}$$

$$R_V = \frac{R_i}{1 + BK} \quad \text{feeding back in shunt}$$

$$R_V = R_i (1 + BK) \quad \text{feeding back in series}$$

### Power Supplies

$$I_{DC} (\text{max}) = I_{SEC} (\text{max}) \times \text{Derating \%}$$

$$V_{avg} = \frac{2V_P}{\pi} \quad V_{RMS} = \frac{V_P}{\sqrt{2}} \quad \text{(justified full-wave rectifier)}$$

$$V_{avg} = \frac{V_P}{\pi} \quad V_{RMS} = \frac{V_P}{2} \quad \text{(unjustified half-wave rectifier)}$$

### Filtering & Regulation

$$V_{rIP} = \frac{V_{rT}}{\tau} = \frac{IT}{C} \quad V_{C_{min}} = V_{DC} = V_P - \frac{V_{rIP}}{2}$$

$$\% \text{ Load Regulation} = \frac{V_{NL} - V_{FL}}{V_{FL}} \times 100 \%$$

$$\% \text{ Line Regulation} = \frac{\Delta V_{FL}}{V_{FL}} \times 100 \% \quad V_{r_{max}} = \frac{V_{rIP}}{2\sqrt{3}}$$

$$P_D (\text{regulator}) = (V_{IN} - V_O) I_O$$

$$V_{IN} = V_O + V_{rIP}$$

### Op Amp Applications

$$\text{Inverting Amp: } A_v = \frac{-R_f}{R_i} \quad R_i = R_1 \quad R_o = 0$$

$$\text{Non-inverting Amp: } A_v = \frac{R_f}{R_1} + 1 \quad R_i = \infty \quad R_o = 0$$

$$\text{Summing Amp: } V_o = V_{O1} A_{v1} + V_{O2} A_{v2} + V_{O3} A_{v3} + \dots$$

$$\text{Difference Amp: } V_o = (V_{INAV} - V_{INV}) \left( \frac{R_f}{R_1} \right)$$

### Butterworth Active Filters

$$A_o = 3 - \alpha \quad f_c = \frac{1}{2\pi RC}$$

### Sampling Theorem

$$f_s \geq 2 f_{(max)} \quad f_{max} (\text{LP maximally flat}) \leq \frac{f_c}{2}$$

### A/D & D/A Conversion













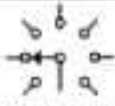


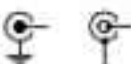

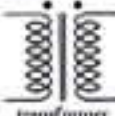





$$n = \text{number of bits}$$



















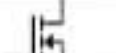






$$\text{Min. Attn.} = 20 \log 2^n$$

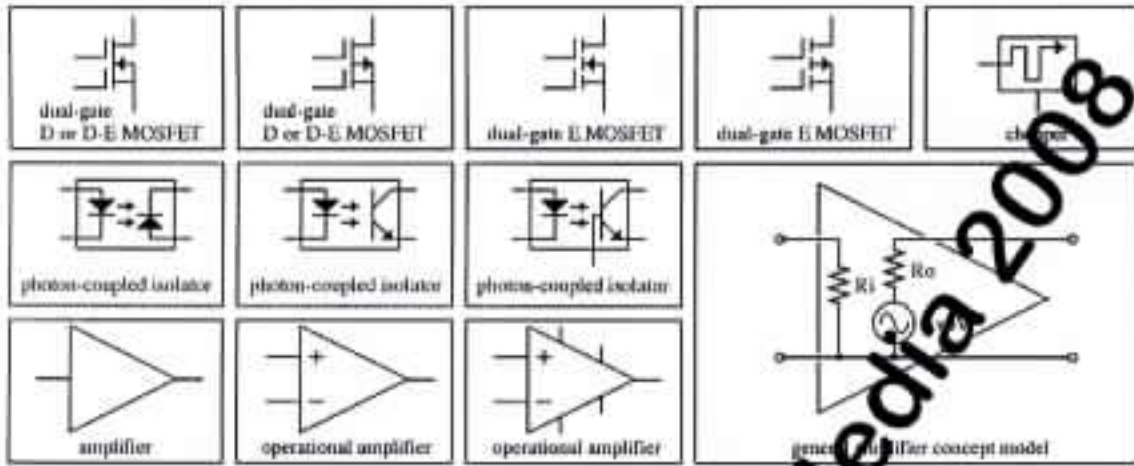
$$V_o = \frac{\text{decimal bit value} \times \text{span width}}{2^n}$$

## Schematic Symbols

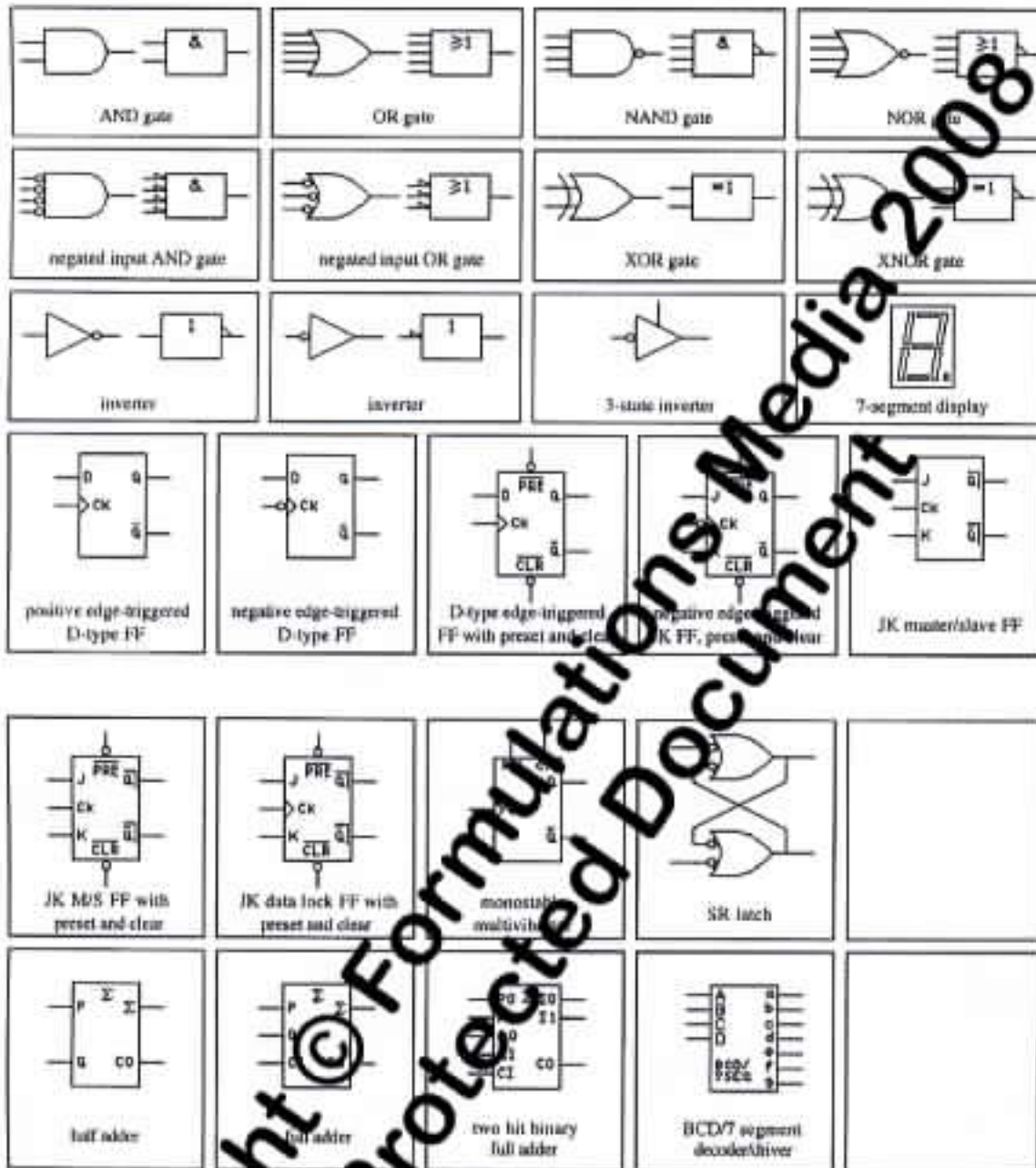
 resistor	 potentiometer	 variable resistor	 thermistor	 photoconductive resistor
 capacitor	 electrolytic capacitor	 variable capacitor	 tantalum capacitor	 feedthrough capacitor
 air-core inductor	 ferrite or powdered iron core inductor	 iron-core inductor	 variable inductor	 variable inductor with movable ferrite core
 variable inductor with movable ferrite core	 inductor with internal resistance	 dc voltage source single cell	 dc voltage source power supply	 photovoltaic cell or photocell
 dc current source	 ac voltage source	 meter movement	 fuse	 circuit breaker
 thermocouple	 multi ground	 chassis ground	 other ground	 magnetic read or write head
 voltmeter	 ammeter	 ohmmeter	 antenna	 loop antenna
 headset or earphones	 dc generator	 dc motor	 ac generator	 ac motor
 motor or actuator	 incandescent lamp	 LED lamp	 dc glow or neon lamp	 ac glow or neon lamp
 two-terminal fluorescent lamp	 speaker	 microphone	 crystal	 crystal filter

 2-wire ac plug	 3-wire ac plug	 SPST switch	 SPDT switch	 SP3T switch
 DPST switch	 DP1TT switch	 DP3T switch	 SPDT slide switch	 DPDT slide switch
 momentary contact switch (NO)	 momentary contact switch (NC)	 SP7T BSM switch	 SP7T MBB switch	 multi-position switch
 2-wire chassis jack	 phone jack	 transformer	 transformer with center-tap secondary	 transformer with multiple secondary windings
 dangerous voltage	 caution	 shielded transformer		

 PN junction diode	 zener diode	 light-emitting diode	 photoconductive diode	 tunnel diode
 Schottky diode	 bi-directional diode or DMAC	 bi-directional diode	 PUT, programmable unijunction transistor	 SCR, silicon controlled rectifier
 thyristor or silicon controlled switch, SCS	 functional gated switch or TRM	 NPN transistor	 PNP transistor	 n-channel JFET
 p-channel JFET	 n-channel D or D-E MOSFET	 p-channel D or D-E MOSFET	 n-channel E MOSFET	 p-channel E MOSFET
 PNP Schottky transistor	 PNP Schottky transistor	 n-type unijunction transistor	 p-type unijunction transistor	 NPN phototransistor



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Preceding symbols conform to the following standards: ANSI Y32, CSA Z99, and IEEE 315 91. Some symbols (inductor with internal resistance, general amplifier concept model, SR latch) are combined from standard symbols.

## American Wire Gauge (AWG) Data Sheet (for annealed copper at 20 °C)

Gauge	Diameter (mm)	Diameter (in.)	Resistance $\Omega$ /km	Resistance $\Omega$ /1000 ft.	Current Capacity
0000	11.68	0.4600	0.1608	0.04901	769 A
000	10.40	0.4096	0.2028	0.06180	710 A
00	9.266	0.3648	0.2557	0.07793	644 A
0	8.252	0.3249	0.3224	0.09827	584 A
1	7.348	0.2893	0.4065	0.1239	540 A
2	6.543	0.2576	0.5128	0.1563	491 A
3	5.827	0.2294	0.6463	0.1970	447 A
4	5.189	0.2043	0.8153	0.2472	408 A
5	4.620	0.1819	1.028	0.3111	374 A
6	4.115	0.1620	1.296	0.3911	344 A
7	3.665	0.1443	1.635	0.4982	317 A
8	3.264	0.1285	2.061	0.6282	292 A
9	2.906	0.1144	2.599	0.7921	27.6 A
10	2.588	0.1019	3.277	0.9989	27.8 A
11	2.305	0.09074	4.134	1.260	29.9 A
12	2.053	0.08081	5.210	1.588	23.8 A
13	1.828	0.07196	6.577	2.006	18.8 A
14	1.628	0.06408	8.284	2.526	14.9 A
15	1.450	0.05707	10.49	3.197	11.9 A
16	1.291	0.05082	13.29	4.016	9.39 A
17	1.150	0.04526	16.76	5.064	7.45 A
18	1.024	0.04030	20.95	6.385	5.91 A
19	0.9116	0.03589	26.41	8.051	4.68 A
20	0.8118	0.03196	33.30	10.15	3.71 A
21	0.7229	0.02846	41.99	12.80	2.95 A
22	0.6439	0.02535	52.91	16.14	2.34 A
23	0.5733	0.02254	66.44	20.36	1.85 A
24	0.5105	0.02006	82.97	25.67	1.47 A
25	0.4547	0.01790	103.2	32.37	1.17 A
26	0.4049	0.01594	127.9	40.81	924 mA
27	0.3607	0.01420	168.9	51.47	733 mA
28	0.3211	0.01264	212.9	64.90	581 mA
29	0.2860	0.01126	268.5	81.83	461 mA
30	0.2548	0.01003	338.6	103.2	366 mA
31	0.2268	0.008968	426.8	130.1	290 mA
32	0.2019	0.008032	538.4	164.1	230 mA
33	0.1792	0.007080	678.8	206.9	182 mA
34	0.1587	0.006205	856.0	260.9	144 mA
35	0.1420	0.005615	1079	329.0	115 mA
36	0.1270	0.005000	1361	414.8	90.9 mA
37	0.1131	0.004453	1716	523.1	72.1 mA
38	0.1007	0.003965	2164	659.6	57.2 mA
39	0.08969	0.003531	2729	831.8	45.3 mA
40	0.07988	0.003145	3442	1049	36.0 mA

\* Current carrying capacity is based upon three insulated conductors in a cable with an ambient temperature of 30°C with a conductor temperature not to exceed 60°C, and assuming a current density of 3.64 mA/CM or 275 CM/A. Wires will get warm when operating at the maximum currents listed in this table. For cooler operation, derate to 25% of listed currents.

## Resistivity & Temperature Coefficients

(for various materials all at 20 °C)

Conductive Materials	Resistivity ( $\rho$ ) ( $\mu\Omega\text{m}$ )	Temp. Coefficient ( $\alpha$ ) ( $^{\circ}\text{C}$ )
Alumel	333.0	$1.2 \times 10^{-5}$
Aluminum	26.2	$3.9 \times 10^{-2}$
Brass	39.0	$2.0 \times 10^{-5}$
Carbon (graphite)	1400.0	$-5.0 \times 10^{-4}$
Chromel	700.0	$1.1 \times 10^{-4}$
Constantan	442.0	$2.0 \times 10^{-4}$
Copper (annealed)	17.2	$3.93 \times 10^{-2}$
Gold	24.4	$3.4 \times 10^{-2}$
Iron	97.1	$5.7 \times 10^{-2}$
Manganin	440.0	$\pm 2.0 \times 10^{-4}$
Mercury (liquid)	958.0	$8.9 \times 10^{-4}$
Monel	420.0	$2.0 \times 10^{-3}$
Nichrome	1000.0	$1.5 \times 10^{-4}$
Nickel	69.0	$7.7 \times 10^{-3}$
Platinum	105.0	$3.0 \times 10^{-2}$
Silicon	2300.0	$-7.5 \times 10^{-2}$
Silver	16.2	$3.8 \times 10^{-2}$
Tungsten	54.8	$4.5 \times 10^{-2}$
Zinc	60.0	$6.9 \times 10^{-3}$
Insulation Materials	Resistivity ( $\rho$ )	
Amber	500 T $\Omega\text{m}$	
Bakelite	10 <sup>12</sup> $\Omega\text{m}$	
Glass	10 <sup>12</sup> $\Omega\text{m}$	
Mica	100 T $\Omega\text{m}$	
Nylon	8 T $\Omega\text{m}$	
Paper	10 G $\Omega\text{m}$	
Paraffin Wax	50 T $\Omega\text{m}$	
Polystyrene	10 P $\Omega\text{m}$	
Rubber	100 T $\Omega\text{m}$	
Teflon	1 P $\Omega\text{m}$	

G =  $1 \times 10^9$  (giga)  
 T =  $1 \times 10^{12}$  (tera)  
 P =  $1 \times 10^{15}$  (peta)  
 E =  $1 \times 10^{18}$  (exa)

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## Relative Permittivity & Dielectric Strength (for various materials)

Dielectric Materials	Relative Permittivity ( $\epsilon_r$ )	Dielectric Strength (V/ $\mu\text{m}$ )
dry air, or vacuum	1.00	3.15
ceramic	3300	3.61
glass	6.16	47.4
mica	6.43	96.5
oil	3.10	14.1
polyethylene	2.69	102
polypropylene	2.35	25.6
rubber	3.28	24.5
teflon	2.37	44

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**Table of Prefixes**

Prefix Symbol	Prefix Name	Prefix Value
E	exa	$1 \times 10^{18}$
P	peta	$1 \times 10^{15}$
T	tera	$1 \times 10^{12}$
G	giga	$1 \times 10^9$
M	mega	$1 \times 10^6$
k	kilo	$1 \times 10^3$
m	milli	$1 \times 10^{-3}$
$\mu$	micro	$1 \times 10^{-6}$
n	nano	$1 \times 10^{-9}$
p	pico	$1 \times 10^{-12}$
f	femto	$1 \times 10^{-15}$
a	atto	$1 \times 10^{-18}$

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## Network Theorem Rules

### Thévenin's Theorem

1. Determine which portion of the circuit will be classified as the load.
2. Remove the load leaving an open circuit.
3. Determine the voltage across the open-circuited load terminals. This is  $V_{TH}$ .
4. Replace each voltage source with a short circuit and each current source with an open circuit.
5. Determine the resistance looking into the load terminals. This is  $R_{TH}$ .
6. The Thévenin equivalent circuit consists of  $V_{TH}$  in series with  $R_{TH}$ .
7. Connect the original load to the Thévenin equivalent circuit and solve as required.

### Norton's Theorem

1. Determine which portion of the circuit will be classified as the load.
2. Remove the load and connect a short circuit to the load terminals.
3. Determine the current through the short circuit. This is  $I_N$ .
4. Remove the short circuit from the load terminals leaving the load terminals open.
5. Replace each voltage source with a short circuit and each current source with an open circuit.
6. Determine the resistance looking into the load terminals. This is  $R_N$ .
7. The Norton equivalent circuit consists of  $I_N$  in parallel with  $R_N$ .
8. Connect the original load to the Norton equivalent circuit and solve as required.

### Superposition Theorem

1. Determine the portion of the circuit, usually one resistor, to which superposition will be applied.
2. Analyze the circuit using one source only while replacing all other voltage sources with short circuits and all other current sources with open circuits.
3. Determine voltage or current for the resistor of interest due only to this one source.
4. Repeat steps 2 and 3 for each source in the circuit.
5. Sum the voltages or currents for the resistor of interest respecting voltage polarities and current directions.
6. The summation results in the correct voltage or current for the resistor in the original circuit.

### Using Thévenin's or Norton's Theorems with Multiple Source Circuits

1. Apply the theorem first until the load is removed (Thévenin's) or replaced with a short circuit (Norton's).
2. Use superposition techniques to find either  $V_{TH}$  or  $I_N$  for the circuit in its present state.
3. Return to the theorem rules to determine  $R_{TH}$  or  $R_N$  (they are the same) as required.
4. Connect the original load to the equivalent circuit and solve as required.

### Mesh Analysis

1. Determine a minimum number of windows for the circuit so as to include all components.
2. Label the current loops within each window as  $I_1, I_2, I_3$  and so forth. Direction does not matter.
3. There cannot be fewer loops than there are windows.
4. Label, within each window, polarities for all voltage drops caused by the indicated currents.
5. Write a Kirchhoff Voltage Law equation for each window to include all component voltages.
6. Reduce the equations to standard form and solve for the currents  $I_1, I_2, I_3$  as required.
7. Currents which solve to be negative will actually flow opposite to the direction chosen in step 2.
8. Where two currents are defined in one component, their values are combined to yield the actual value.

### Nodal Analysis (Classical Method)

1. Define a reference point in the circuit. This is usually at the bottom of the schematic diagram.
2. Label all voltage nodes in the circuit (even if they are known voltages) as  $V_1, V_2, V_3$  and so forth.
3. Develop the standard equation forms shown below for three unknown nodes.

$$\begin{array}{r}
 + (\Sigma \text{self } G \text{ at } 1) V_1 - (\Sigma \text{mutual } G_{12}) V_2 - (\Sigma \text{mutual } G_{13}) V_3 = \Sigma I \text{ at } 1 \\
 - (\Sigma \text{mutual } G_{21}) V_1 + (\Sigma \text{self } G \text{ at } 2) V_2 - (\Sigma \text{mutual } G_{23}) V_3 = \Sigma I \text{ at } 2 \\
 - (\Sigma \text{mutual } G_{31}) V_1 - (\Sigma \text{mutual } G_{32}) V_2 + (\Sigma \text{self } G \text{ at } 3) V_3 = \Sigma I \text{ at } 3
 \end{array}$$

4. Note that " $\Sigma \text{self } G \text{ at } 1$ " means the sum of the self-conductances at node 1.  
 Note that " $\Sigma \text{mutual } G_{21}$ " means the sum of the mutual conductances between nodes 1 and 2.  
 Note that self-conductance refers only to resistors which directly connect to the stated node.  
 Note that mutual conductance refers only to resistors which connect between the stated nodes.  
 Note that all self-conductance terms are positive and all mutual conductance terms are negative.  
 Note that " $\Sigma I \text{ at } 1$ " means the sum of the current sources at node 1.  
 Note that current sources entering a node are positive, and leaving a node are negative.  
 Note the symmetry in similar terms:  $\Sigma \text{mutual } G_{12} = -\Sigma \text{mutual } G_{21}$ .
5. Reduce the equations to standard form and solve for  $V_1, V_2$  and  $V_3$  as required.

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## SI Notation Rules

The following rules illustrate some of the commonly-seen errors in the use of the SI system of notation. These errors are often seen in technical documents to an extent inversely proportional to the length of the writing process undertaken in the creation of the document. If these errors are avoided, little else can go wrong.

- Derived units formed through division use "per" when accompanying units are written in full or "/" when accompanying units are abbreviated.

**CORRECT:** kilometres per hour  
km/h

**WRONG:** kilometres/hour  
km per hour

- Quantities abbreviated by unit symbols are the same in singular or in plural. Unabbreviated quantities may be pluralized.

**CORRECT:** 250 km  
eighty kilometres

**WRONG:** 250 kms  
80 km's

- Periods are not used after units except at the end of a sentence.

**CORRECT:** A voltage of 15 V was present.  
15 V was present at the switch.

**WRONG:** A voltage of 15 V. was present.  
15 V. was present at the switch.

**EXCEPTIONS:** Some non-SI units, still in use, use periods. Examples are: ft. in. mi. lb.

- Negative exponents may be used to indicate symbols in the denominator of an expression.

**CORRECT:** 50 kmh<sup>-1</sup>  
100 m/s<sup>2</sup> or 100 m/s<sup>2</sup>

**WRONG:** 50 km ph  
100 m/s/s

- Leave a space between numerals and the units, but not between prefixes and units.

**CORRECT:** 16.8 mA

**WRONG:** 16.8mA 16.8m A  
16.8 m A

- The Celsius temperature scale (not an SI unit) previously known as centigrade, uses the degree sign (°). The SI unit, kelvin, does not use this symbol. Note that kelvin uses an uppercase K as its unit symbol. One Celsius degree is equal to one kelvin.

**CORRECT:** 0° C = 273.15 K  
10° C = 283.15 K

**WRONG:** 0° C = 273.15 k  
0°C = 273.15 K

- When writing numbers which are less than one, a zero should precede the decimal point. This is designed to help make the decimal point more obvious to the reader.

**CORRECT:** 0.381

**WRONG:** .381

- Correctly use commas and decimal points for the geographical area in which you are located. For North America, except Québec, decimal points are used as the unity digit marker and commas may be used as separators. In Québec and some places in Europe, the unity digit marker is a comma. For North America:

**CORRECT:** 15.7 kΩ  
\$ 13.26

**WRONG:** 15,7 kΩ  
13,26 \$

9. Use spaces to break up large blocks of numbers in groups of three in either direction from the decimal point. Commas are still widely used in North America as spacers.

CORRECT: 48 316.748 21                      WRONG: 48316.74821  
 48,316.748 21                                  4,316.748,21

10. Only one prefix may be used with a unit symbol. In the past the use of multiple prefixes, such as micro micro in place of pico was widely accepted. This is no longer the case.

CORRECT: 390 pF                                  WRONG: 390 μμF  
 580 μm    580 mmμ

11. For derived units use only one prefix and attach it to the numerator, not to the denominator. There are some exceptions to this rule which are in widespread use. The two technically wrong examples are widely used.

CORRECT: 16.3 mΩ/m                              WRONG: 16.3 Ω/km  
 500 kV/s    500 V/μs

12. The use of Engineering Notation where powers are always a multiple of three and the number is  $\geq 1$  but  $< 1000$  is highly recommended where units are involved. Where no units are present scientific notation is preferred but only for very large or very small numbers.

CORRECT: 18.3 mA                                  WRONG: 0.0183 A  
 1.2 kΩ    1.20 Ω  
 Ap = 1580    Ap =  $1.58 \times 10^3$  (cumbersome)  
 Ap =  $6.50 \times 10^6$                                       Ap = 6,500,000 (cumbersome)

13. Where no units are present, it is incorrect to use a prefix. Prefixes are intended only for use alongside a unit symbol, never to stand alone. On schematic diagrams, values such as 68 k may be shown in place of 68 kΩ only where the legend indicates all resistor values are in ohms.

CORRECT: Av = 1250                                  WRONG: Av = 1.25 k

14. Values are assumed to be positive unless written with a negative sign so it is redundant to include the positive sign unless there is a valid reason to draw attention to the polarity.

CORRECT: 54.8 V                                      WRONG: +54.8 kV  
 138 V-    138 V-

15. The SI system spells the word "metre" where it is used in the context of a distance and uses "meter" where an instrument is involved.

CORRECT: The length is five metres.  
 A voltmeter was used.

WRONG: The length is five meters.  
 A voltmeter was used.

# Color Codes

silver or gold helps orient the resistor

tolerance: white:  $\pm 5\%$

multiplier: yellow: 4

2nd digit: grey: 8

1st digit: brown: 6

6 8 0000  $\Omega \pm 5\%$

680 k $\Omega \pm 5\%$

680 k $\Omega \pm 34\text{ k}\Omega$

646 k $\Omega$  to 714 k $\Omega$

33000  $\Omega \pm 5\%$  200 V

330 nF

0.33  $\mu\text{F}$

2nd digit: multiplier: orange: 3, 3rd digit: 3, 4 zeroes

tolerance: white:  $\pm 10\%$

voltage: red: 200 V

Note that the double orange band is wider than individual bands. Also, note that there is no separating line between the orange bands. This may also occur with a double red band.

black 0 40%

brown 1

red 2 200 V

orange 3 300 V

yellow 4 40%

green 5 500 V

blue 6 600 V

violet 7

grey 8 800 V

white 9 900 V

gold 0.1 0.5%

silver 0.01 10%

gold or silver as a multiplier

black 0 40%

brown 1

red 2 200 V

orange 3 300 V

yellow 4 40%

green 5 500 V

blue 6 600 V

violet 7

grey 8 800 V

white 9 900 V

gold 0.1 0.5%

silver 0.01 10%

gold or silver as a multiplier

## Capacitor Identification



Film Capacitor – Values less than 1 are in  $\mu\text{F}$ . Values greater than 1 are in pF. This capacitor is 1000 pF which is 1.0 nF, and is rated for 400 V.



Ceramic Capacitor – The position of the prefix locates the decimal point. This case is 4.7 pF. One coded as 471 or N22 would be 0.22  $\mu\text{F}$  or 220 pF.



Film Capacitor – This method of coding indicates the first two digits, followed by the number of zeros, with the value being in units of pF. This case is 47000 pF or 47 nF.



Film Capacitor – This value is shown in raised relief as 0.047 and is in  $\mu\text{F}$  if the number is  $<1$  or in pF if  $>1$ . This example is 0.047  $\mu\text{F}$  or 47 nF.

Film Capacitor – These types are usually in  $\mu\text{F}$ , but may be a three-number code as above, or the code number may be printed, for example is 18 followed by 1 zero, or 180 pF. A code such as 680 could mean 68 pF or 6.8 pF and should be measured to be sure of its value.



Film Capacitor – Color-coded in pF starting at the top. This case has a double orange band and is 33 followed by 0000, which is 330000 pF, or 330 nF. There may be a similar double-wide red band.



Electrolytic Capacitor – Values are generally printed on the component along with the voltage rating which is often critical, important as it must not be exceeded. The circled negative points to the negative lead on the right. Some have (+) markings on the positive end. This capacitor must be connected with the correct polarity or it may explode.



Non-Polarized Capacitor – This type may be connected with either polarity even though it has a large value of capacitance.



Electrolytic Capacitor – The dark band points towards the negative lead. This example is 0.1  $\mu\text{F}$  or 100 nF. It could also be coded as  $\mu\text{F}10$  for the same value. A value coded 6 $\mu$ 8 would be 6.8  $\mu\text{F}$ .